

March 19, 2024

Junior Division: Grades 7–9

Form: **T**

Bubble in clearly the single best choice for each question you choose to answer.

- 1. What is the correct time exactly 540 seconds after midnight?
 - (A) 12:09 p.m.
 - (B) 12:09 a.m.
 - (C) 9 p.m.
 - (D) 9 a.m.
 - (E) 12:54 a.m.
- The sum of four consecutive even integers is 148. What is the **sum** of the digits of the smallest of the four?
 - (A) = 6
 - (B) 7
 - (C) 9
 - (D) 12
 - (E) 14
- 3. Kim plays basketball for her school. Her freethrow shooting percentage for the season was 75% exactly before today. During tonight's game she makes all five free throws, bringing her percentage up to 80%. How many free throws has Kim made on the season (including tonight)?
 - (A) 20
 - (B) 22
 - (C) 24
 - (D) = 25
 - (E) 28

- 4. Towns A, B, and C are at the corners of a triangle with equal sides. A car travels at constant speeds from A to B at 30 mph, from B to C at 40 mph, and from C back to A at 60 mph. What is the average speed for the round trip?
 - (A) 40 mph
 - (B) 43 mph
 - (C) 45 mph
 - (D) 48 mph
 - (E) 50 mph
- 5. Four rings of different sizes are stacked on one of three posts in ascending order (smallest on top). You are able to move one ring at a time (taking the top ring from one post and moving it to another post), but you may never place a larger ring on a smaller ring. What is the minimum number of moves required to move the entire stack to a different post?



- 6. The product of the lengths of the diagonals of a square is 72. What is the length of the sides of the square?
 - (A) 4
 - (B) 5
 - (C) 6
 - (D) 8
 - (E) 9

- 7. The shadow cast by a tall tree is 6 m long. At the same time of day and at the same location, an upright meter stick casts a shadow of 20 cm. How tall is the tree?
 - $20\,\mathrm{m}$ (A)
 - (B) $24\,\mathrm{m}$
 - (C) $27\,\mathrm{m}$
 - (D) $28\,\mathrm{m}$
 - (E) $30\,\mathrm{m}$
- 8. The sum of the first n counting numbers is 210: $1 + 2 + 3 + \dots + n = 210$. Find *n*.
 - (A)14
 - (B)16
 - (C)17
 - (D)20
 - (E)24
- 9. In the following diagram, lines l and m are parallel. Find the measure of angle x.



10. Compute the following sum in base 2.

	1	1	0	1	1	0	1
+		1	1	1	0	1	1

- (\mathbf{A}) 10001100
- (B)11010111
- (C)10110010
- (D)11011101
- (E)10101000

- 11. For the function $f(x) = x^2 + 2x 5$, compute the value of f(f(f(1))).
 - (A)-5
 - (B)5
 - (C)10
 - (D)12
 - (E)115
- 12. One cubic centimeter is equal to how many cubic millimeters?
 - (\mathbf{A}) 10
 - (B)100
 - (C)1000
 - (D) $10\,000$
 - (E)1000000
- 13. One side of the gray square is increased by 3 cm while its adjacent side is decreased by $2 \,\mathrm{cm}$. The perimeter of the resulting rectangle is 22 cm. What is the area of the original gray square?
 - $9\,\mathrm{cm}^2$ (A)
 - $16\,\mathrm{cm}^2$ (B)
 - $25\,\mathrm{cm}^2$ (C) $64\,\mathrm{cm}^2$

(D)



- $121\,\mathrm{cm}^2$ (E)
- 14. Find the intersection point of the diagonals of the parallelogram ABCD for A(2, -1), B(5,2), C(7,-3), and D(4,-6).
 - (A) $(\frac{9}{2}, -2)$
 - (B) (4, -2)
 - (C) (5, -3)
 - (D) $(\frac{9}{2}, -3)$
 - $(\frac{9}{2}, -\frac{5}{2})$ (E)

- 15. Three disks of radius 1 cm are mutually tangent as in the figure below. A rubber band is wrapped around the outside of the group. Find the total length of the band in cm.
 - (A) $3 + \pi$
 - (B) 3π
 - (C) $3 + 2\pi$
 - (D) 6π
 - (E) $6 + 2\pi$

16. What is the area of the triangle?

- (A) 12
- (B) 12.5
- (C) 20
- (C) 25 (D) 25
- (E) 40
- 17. The number 6545 can be written as a product of a pair of positive two-digit integers. What is the sum of the two integers?
 - (A) 156
 - (B) 162
 - (C) 187
 - (D) 238
 - (E) 166

- 18. Which whole number is closest to the ratio?
 - $\begin{array}{r}
 \frac{10^{2023} + 10^{2025}}{10^{2024} + 10^{2024}} \\
 1 \\
 2 \\
 4 \\
 5 \\
 10
 \end{array}$

19. Find the median: 2, 5, 10, 8, 2, 4, 9, 9, 7, 9.

(A) 7

 (\mathbf{A})

(B)

(C)

(D)

(E)

- (B) 7.5
- (C) 10
- (D) 9
- $(E) \quad 6.5$
- 20. Going only right or down, how many different ways are there to get from point A (upper left corner) to point B (lower right corner) of the 3 × 4 grid below?





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